

## Processor Scheduling (INOI 2019 Problem 1)

There are  $N + M$  jobs waiting to be run on a processor.  $N$  of these are **classified** jobs:  $C_1, C_2, \dots, C_N$ , and the other  $M$  are **public** jobs:  $P_1, P_2, \dots, P_M$ . There can only be one job running on the processor at any given millisecond (ms). Once the processor starts running a job, it has to finish it completely before starting any other job.

$C_i$  takes time  $q_i$  milliseconds (ms) to finish. Also, for  $1 \leq i \leq N$ ,  $C_i$  can be started **only after**  $C_1, C_2, \dots, C_{i-1}$  have finished.

$P_j$  takes  $p_j$  ms to finish. These jobs can be run in any order. The classified and public jobs can also be interleaved in any order. However, sources have reported that for all  $1 \leq j \leq M$ , there may be an interrupt signal sent to the processor by an alien spaceship at time  $t_j$ . In order to remain on good terms with the aliens, the processor is required to be running the public job  $P_j$  at time  $t_j$ . In other words, each of the  $M$  public jobs need to be scheduled such that for  $1 \leq j \leq M$ , if  $P_j$  starts at the  $s_j$ -th millisecond, then  $s_j \leq t_j < s_j + p_j$ .

You want to finish all the jobs as soon as possible. You can start assigning jobs from time 1. Please find the minimum time (in ms) by which all the  $N + M$  jobs can be finished. If it is not possible to finish all the jobs while satisfying the rules, output  $-1$  instead.

### Input:

- First line will contain  $T$ , the number of testcases. Then the testcases follow.
- The first line of each test case contains two integers  $N$  and  $M$ , the number of classified and public jobs respectively.
- The second line contains  $N$  space separated integers  $q_1 \dots q_N$ .
- The third line contains  $M$  space separated integers,  $p_1 p_2 \dots p_M$ .
- The fourth line contains  $M$  space separated integers,  $t_1 t_2 \dots t_M$ .

### Output:

For each testcase, output in a single line the minimum time in ms needed to finish all the jobs. If it is not possible to finish all the jobs output  $-1$  instead.

### Constraints

- $1 \leq T \leq 10$
- $0 \leq N \leq 5000$
- $0 \leq M \leq 5000$
- $1 \leq N + M$
- $1 \leq q_i, p_i, t_i \leq 10^9$

### Subtasks

- **Subtask 1:** 10 points :  $N \leq 10, M \leq 10$
- **Subtask 2:** 16 points :  $N = 0$
- **Subtask 3:** 13 points:  $p_i = 1$  for each of the  $M$  public jobs.
- **Subtask 4:** 61 points: No further constraints

### Sample Input:

```
2
4 2
3 4 1 2
3 2
4 9
4 2
3 4 1 1
3 2
4 9
```

**Sample Output:**

16

15

**Explanation:**

**Testcase 1:** We can start  $C_1$  at  $t = 1$ . Because its duration is 3ms, it will take up the times 1, 2 and 3. Then at  $t=4$ , we can start  $P_1$ . It will take up  $t=4, 5$ , and 6. Then we leave  $t=7$  free, and at  $t=8$ , we start  $P_2$ , which will end at  $t=9$ . Then at  $t=10$ , we start  $C_2$  which will end at  $t=13$ . Then at  $t=14$ , we start  $C_3$  which finishes at that very second. And finally, at  $t=15$ , we start  $C_4$ , which ends at  $t=16$ . Note that at  $t_1$  (ie.  $t = 4$ ),  $P_1$  was being executed, and at  $t_2$  (ie.  $t = 9$ ),  $P_2$  was being executed.

This is the best we can do, and hence the answer is 16.

## Interesting Sequences (INOI 2019 Problem 2)

You are given  $N$  integers in an array:  $A[1], A[2], \dots, A[N]$ . You also have another integer  $L$ .

Consider a sequence of indices  $(i_1, i_2, \dots, i_k)$ . Note that a particular index can occur multiple times in the sequence, and there is no order in which these indices have to occur.  $(i_1, i_2, \dots, i_k)$  is a sequence of size  $k$ . It is said to be an *Interesting* sequence, if  $A[i_1] \geq A[i_2] \geq \dots \geq A[i_k]$ .

The *Cost* of an Interesting sequence  $(i_1, i_2, \dots, i_k)$ , is defined to be the minimum absolute difference between any two adjacent indices. In other words, the Cost is  $\min\{|i_2 - i_1|, |i_3 - i_2|, \dots, |i_k - i_{k-1}|\}$ .

Your job is to consider the Costs of all the Interesting sequences of size  $L$  associated with the given array, and output the maximum Cost. Note that you can show that there is always at least one Interesting sequence for the given constraints.

### Input

- The first line contains a single integer,  $T$ , which is the number of testcases. The description of each testcase follows.
- The first line of each testcase contains two space separated integers:  $N$  and  $L$ .
- The second line of each testcase contains  $N$  space separated integers:  $A[1], A[2], \dots, A[N]$ .

### Output

- For each testcase, output the answer in a new line.

### Constraints

- $1 \leq T \leq 3$
- $1 \leq A[i] \leq 10^9$
- $2 \leq L \leq 10^9$

### Subtasks

- **Subtask 1:** 7 points
  - It is guaranteed that  $A[1] > A[2] > \dots > A[N]$
  - Note that the above condition implies that all elements are distinct.
  - $1 \leq N \leq 500$
- **Subtask 2:** 7 points
  - It is guaranteed that  $A[1] \geq A[2] \geq \dots \geq A[N]$
  - $1 \leq N \leq 500$
- **Subtask 3:** 14 points
  - It is guaranteed that all elements are distinct.
  - $1 \leq N \leq 500$
- **Subtask 4:** 14 points
  - $1 \leq N \leq 500$
- **Subtask 5:** 25 points
  - It is guaranteed that all elements are distinct.
  - $1 \leq N \leq 3000$
- **Subtask 6:** 33 points
  - $1 \leq N \leq 3000$

### Sample Input

```
1
6 3
2 4 1 12 3 5
```

### Sample Output

```
3
```

### **Explanation**

We are looking for Interesting sequences of length 3. Some of them are: - (4, 2, 3): This is Interesting because  $A[4] \geq A[2] \geq A[3]$ . Its cost is  $\min\{|2 - 4|, |3 - 2|\} = 1$ . - (5, 1, 1): Cost is 0. - (2, 2, 2): Cost is 0. - (6, 1, 3): Cost is 2. - (6, 2, 5): Cost is 3.

There are other Interesting Sequences of length 3 as well. But if you list them all out, you'll see that the maximum Cost is 3. Hence the answer is 3.

## **INOI 2019 Cutoffs**

- Class 12: 39/200
- Class 11: 33/200
- Class 10: 29/200
- Class 9 and below: 26/200